

FIRST SEMESTERAPRIL/MAY 2013PH 303 NUCLEAR PHYSICS

Time: 1 hour

Answer ALL Questions

1. What is meant by the term "nuclear binding energy".

Explain in which way an atomic nucleus behaves like a liquid drop model.

The semi-empirical mass formula (SEMF) for a nucleus with atomic mass number  $A$  and atomic number  $Z$  can be expressed by

$$M_A(A, Z) = Zm_p + (A - Z)m_n - a_v A + a_s A^{\frac{1}{3}} + a_c \frac{Z(Z-1)}{A^{\frac{1}{3}}} + a_{asy} \frac{(A - 2Z)^2}{A} + \delta$$

Explain the physical interpretation of the terms corresponding to the parameters  $a_v$ ,  $a_s$ ,  $a_c$ ,  $a_{asy}$ , and  $\delta$ .

- (i) Show that for a constant  $A$  the SEMF can be reduced to a quadratic function of  $Z$  given by

$$M_A(A, Z) = \alpha A + \beta Z + \gamma Z^2 \mp \delta$$

where  $\alpha$ ,  $\beta$ ,  $\gamma$  and  $\delta$  are functions of  $A$ .

- (ii) Show that the masses  $M_A(A, Z)$  for a particular set of isobars with an odd  $A$  value takes the following form

$$M_A(A, Z) = M_A(A, Z_0) + \chi(Z - Z_0)^2$$

where  $Z_0$  is the atomic number of the most stable isobar.

- (iii) Hence show that the energy released between neighbouring isobars in  $\beta^-$  decay is

$$Q_{\beta^-} = 2\gamma \left[ Z_0 - Z - \frac{1}{2} \right].$$

For a typical  $\beta^-$  decay, illustrate the variation of  $Q_{\beta^-}$  on a scheme of  $M_A(A, Z)$  versus  $Z$ .

2. Define scattering process and elastic scattering in nuclear physics.

In a laboratory reference frame, an incident particle of mass  $m_a$  and kinetic energy  $E_a$  is collides with a target nucleus  $X$  which is at rest. A residual nucleus  $Y$  of mass  $m_Y$  and kinetic energy  $E_Y$  results from the collision together with the emission of a product particle of mass  $m_b$  and kinetic energy  $E_b$  at an angle of  $\theta$  to the direction of the incident particle. Under non-relativistic condition, show that the  $Q$ -value of the reaction is given by

$$Q = \left(\frac{m_a}{m_Y} - 1\right) E_a + \left(\frac{m_b}{m_Y} + 1\right) E_b - \frac{\sqrt{4m_a m_b E_a E_b}}{m_Y} \cos \theta.$$

The  $\alpha$  particles of kinetic energy 7.70 MeV collides with  $^{14}_7\text{N}$  target nuclei to produce  $^{17}_8\text{O}$  residual nuclei and protons. The protons are emitted at  $90^\circ$  to the beam of  $\alpha$  particles are found to have kinetic energy 4.44 MeV. Determine the  $Q$  value of the reaction.

Given that the

Mass of  $\alpha$  particle  $m_\alpha = 4.002604$  a.m.u

Mass of proton  $m_p = 1.007825$  a.m.u

Mass of oxygen  $m_O = 15.990523$  a.m.u and

1 a.m.u =  $931.5 \text{ MeV}/c^2$