



EASTERN UNIVERSITY, SRI LANKA
DEPARTMENT OF MATHEMATICS

INTERNAL DEGREE EXAMINATION IN SCIENCE - 2008/2009

SECOND YEAR FIRST SEMESTER (March/May, 2016)

~~EXTMFAM 215~~ AM 215 - CLASSICAL MECHANICS II
(REPEAT)

Answer all Questions

Time: One hour

With the usual notations, obtain the following equations for a common catenary:

(a) $s = C \tan \psi$;

(b) $y = C \sec \psi$;

(c) $T = wy$;

(d) $y^2 = s^2 + c^2$.

A uniform flexible chain of length ℓ and weight per unit length ω , rest in a vertical plane with length $k\ell$ ($0 < k < \ell$) in contact with the smooth plane inclined at an angle α to the horizontal and upper end of the chain is attached to a point P . Show that the tension at P is $\omega\ell\{1 - k(2 - k)\cos^2\alpha\}^{1/2}$ and find the horizontal, vertical distance of P from lower end.

2. If S and M are shearing force and bending moment respectively at a point on a uniformly loaded beam, then prove that

$$\frac{dS}{dx} = -\omega \quad \text{and} \quad \frac{dM}{dx} = S$$

where ω is the weight per unit length of the beam.

State the Bernoulli-Euler law of flexure.

A uniform elastic beam AB of length $3a$, weight W and flexural rigidity B is clamped horizontally at its ends, which are at the same horizontal level. Two concentrated loads, W and $2W$ are placed at the points of trisection of the beam with the $2W$ load near to A . Show that reaction at A and B are $\frac{95W}{54}$ and $\frac{121W}{54}$ respectively. Find also bending moment at each point.